

# Spatial and Temporal Processing for a Compact Landmine Detection Radar

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# Outline



- Introduction & Motivation
- Our Approach
- A Compact Landmine Detector
- Experiments and Results
- Optimum Signal Processing Algorithms
- Conclusions & Future Work



# Landmine Detection – The Challenge

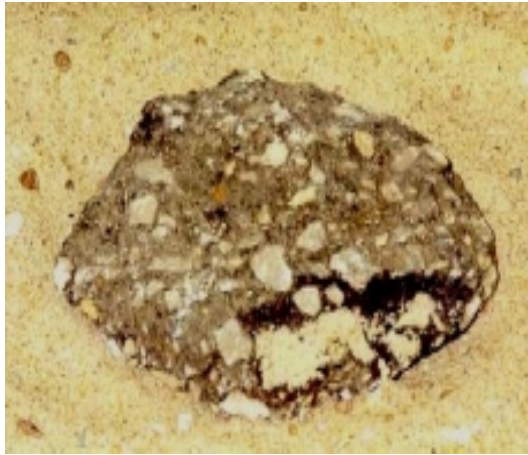


- UN estimates 70 million mines buried all over the world.
- Challenges in Landmine Detection
  - Clearance Rate
  - Probability of False alarm ( $P_{FA}$ ) and Missed detection ( $P_M$ ).
- Landmine Detection Schemes use
  - Metal Detectors.
  - Infra Red Sensors.
  - Chemical Sensors.
- Efficient Landmine Detection Scheme:  
High  $P_D$  and also a low  $P_{FA}$ .





## Our Approach



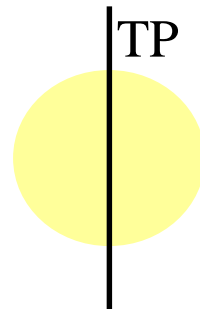
- Is there a property in landmines which is absent in clutter?
- Mines are symmetric and clutter is asymmetric.
- Landmines exhibit reflection symmetry.
- Reflection Symmetry?



# Symmetry in Landmines



- Top View of a landmine



- TP is Target Reflection Symmetric Plane.
- How can we detect Symmetry in Landmines?
- **Our Approach** : Use Ground Penetrating Radar (GPR).
- GPR can be used for detecting subsurface target, but....
- How can symmetry be established with GPR?



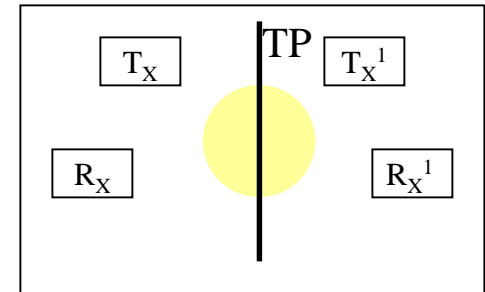
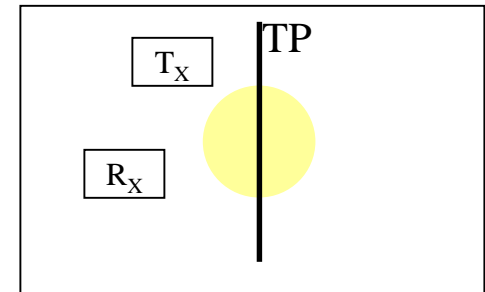
# Bistatic Measurements



- Bistatic Measurement  $T_X-R_X$ .
- Target has reflection Symmetry:
  - Record measurement  $T_X-R_X$ .
  - Reflect the target about TP.
  - Record measurement  $T_X-R_X$  again.
- Reflect the bistatic measurement  $T_X-R_X$ .
  - TP is also Measurement Reflection Symmetric Plane.
- Identical Bistatic measurements  $y_1(t)$  and  $y_2(t)$ .

$$x_1(t) = w(t)y_1(t)$$

$$x_2(t) = w(t)y_2(t)$$



**Mirrored Bistatic Observation Pair**



# Target Detection and Classification



- Is a subsurface target present?

$$\text{sum}(\Sigma) = \int |\mathbf{x}_1(t) + \mathbf{x}_2(t)|^2 dt$$

- Is the subsurface target symmetric?

$$m = \frac{\int |\mathbf{x}_1(t) - \mathbf{x}_2(t)|^2 dt}{\int |\mathbf{x}_1(t) + \mathbf{x}_2(t)|^2 dt} = \frac{\int |\mathbf{x}_1(t) - \mathbf{x}_2(t)|^2 dt}{\text{sum}(\Sigma)}$$

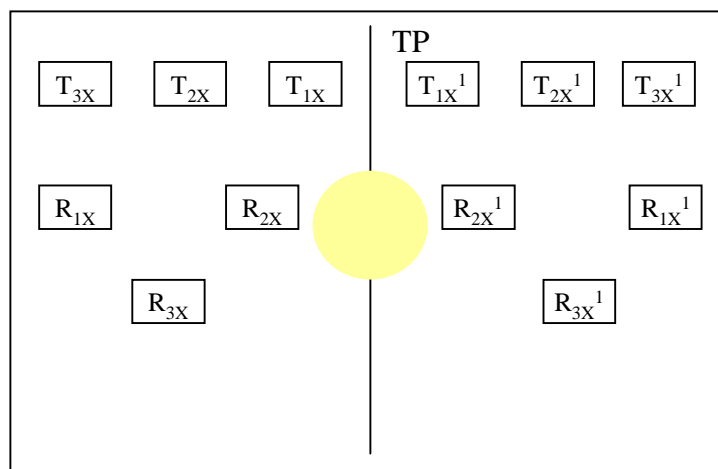
- Typical values for  $m$  coefficient
  - Low  $m$  values for symmetric targets.
  - For asymmetric targets: ranges from low to high values.
- Is one  $m$  value sufficient for Target classification?



# Target Detection and Classification



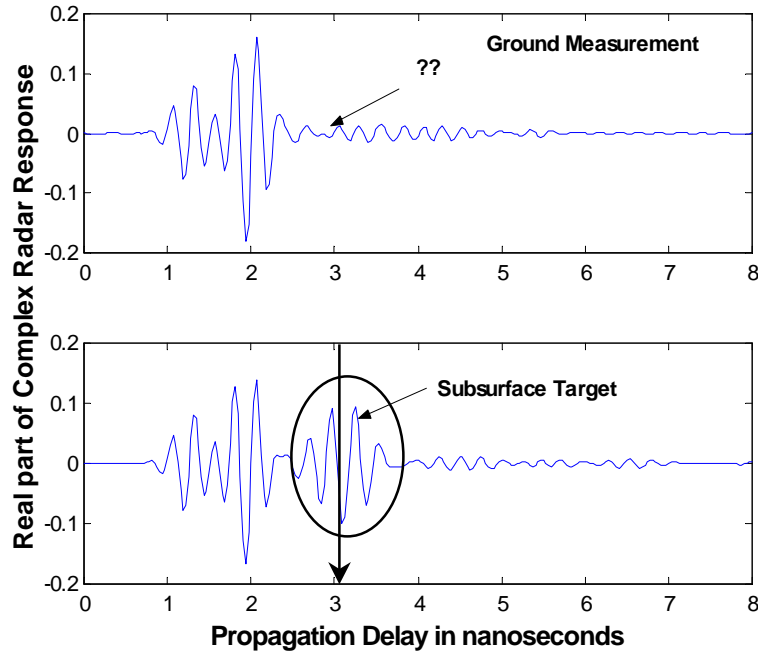
- Single  $m$  coefficient  $\Rightarrow$  High  $P_{FA}$ .
- How many  $m$  coefficients are needed?
  - Higher the number  $m$  values, higher is the confidence level in target classification.
- Solution: Collect many mirrored observation pairs.



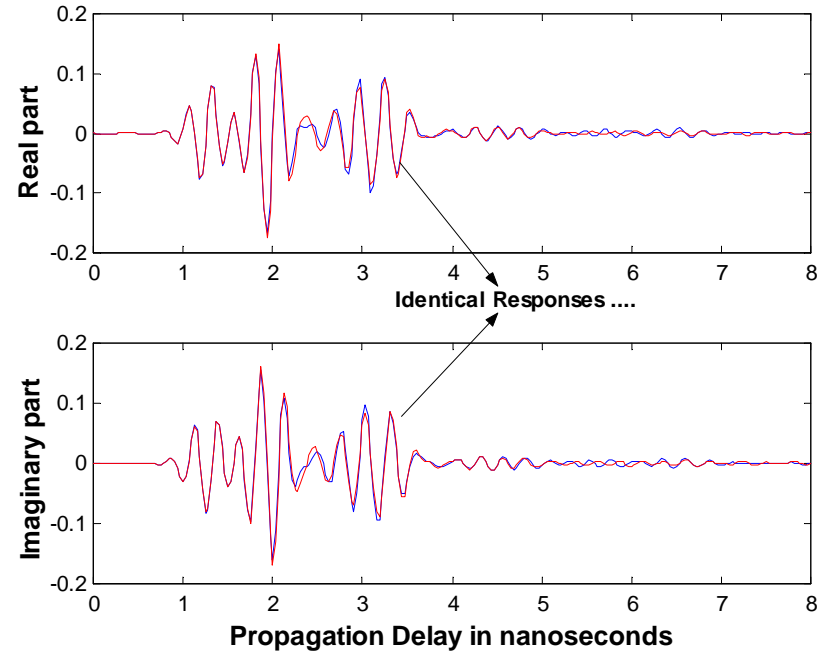




# Initial Results



Subsurface target detected based on electromagnetic scattering.



- Complex radar response  $y_1(t)$
- Complex radar response  $y_2(t)$

Symmetry in subsurface targets manifests itself as identical scattering.



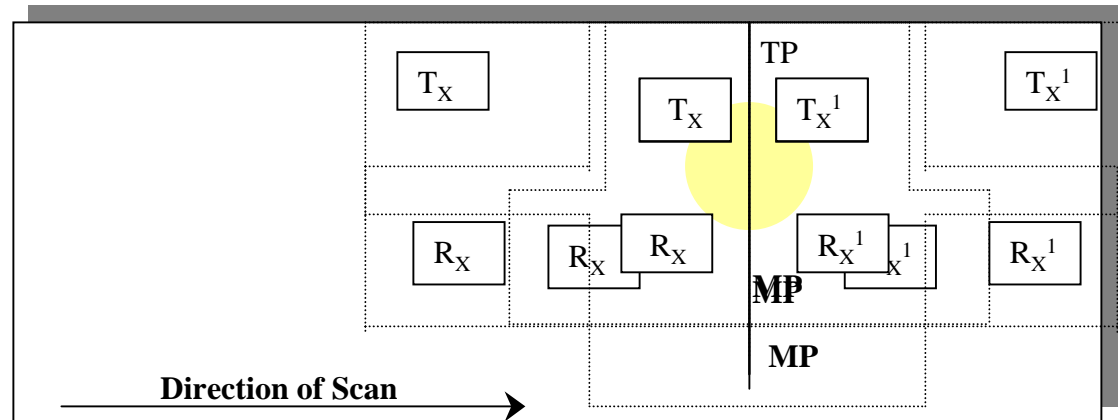
## A Compact Landmine Detector



# Handheld Model



- Possible Handheld model (Top View)



- TP is the target reflection symmetric plane.
- MP is the measurement reflection symmetric plane.
- The combination  $T_X-R_X$   $T_X^{-1}-R_X^{-1}$  is called a *Sensor Geometry*.
- MP for every point in the scan: *Measurement Plane*

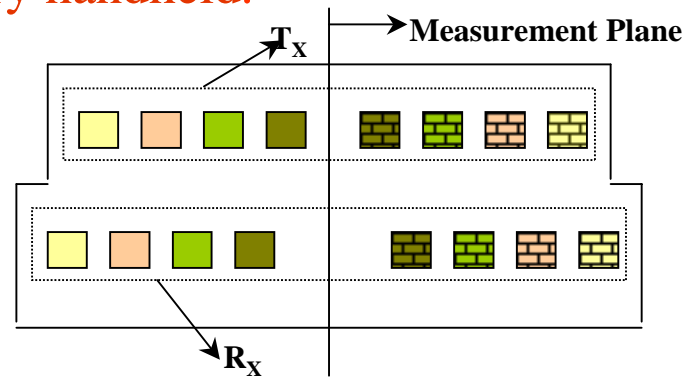


# Multiple Sensor Geometry Handheld



- Scan with a single Sensor geometry
  - Target classification based on one  $m$  value.
  - $P_{FA}$  can be high.
- Solution
  - Repeat scans with different sensor geometries.
  - Develop a **Multiple Sensor Geometry handheld.**

- $N$  sensor geometries  $\Rightarrow N$   $m$  values  
for classifying the target.



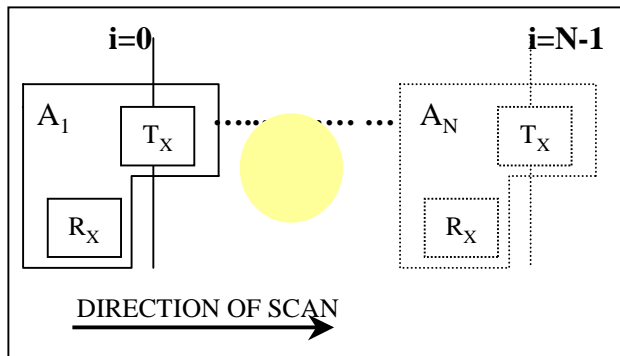
- Higher  $N$  lesser the  $P_{FA}$  ...but greater the complexity.



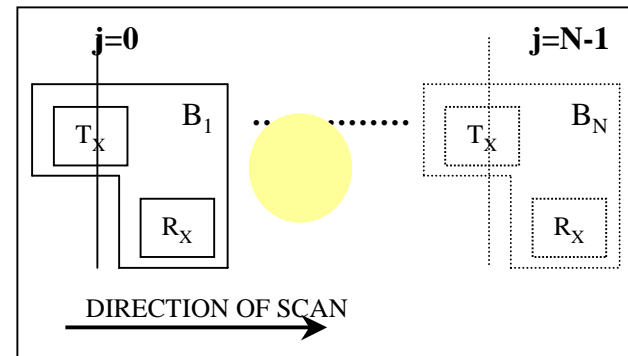
# Data Collection Scheme



- The data collection scheme should
  - reduce the complexity greatly.
  - synthesize Multiple Sensor Geometry Handheld.
- The data collection scheme consists of two scans.



$A_i$  : bistatic measurement at location  $i$



$B_j$  : bistatic measurement at location  $j$

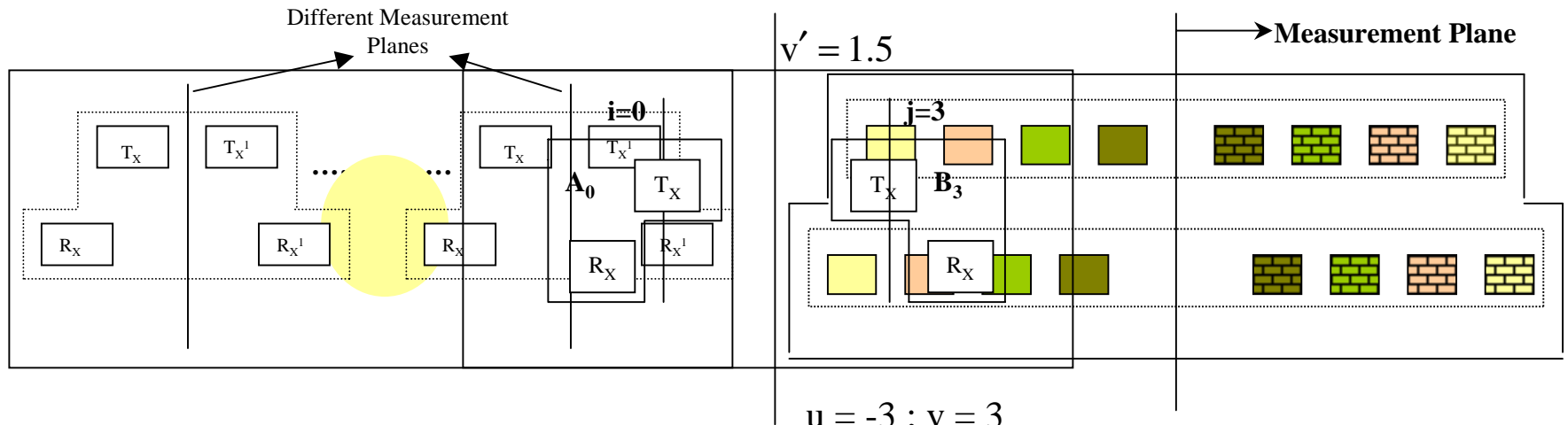
- Synthesize Multiple sensor geometry handheld!! How?



# Synthesizing Multiple Sensor Geometry Handheld



- Reconstruct Multiple sensor geometry handheld
  - Combine  $A_i$  and  $B_j$  to form mirrored bistatic observation pairs.
  - $u = i-j$  defines the sensor geometry.
  - $v = i+j$  defines the measurement plane.



Multiple measurement planes for a single sensor geometry ( $u$  is constant).

Multiple sensor geometries for a single measurement plane ( $v$  is constant)



# Expected Results

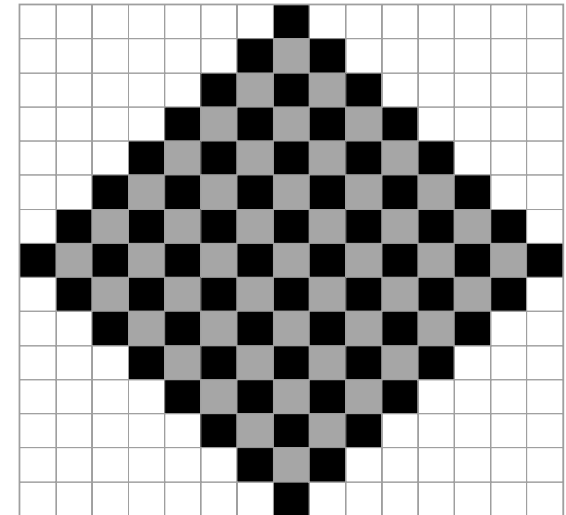


- For each sensor geometry-measurement plane combination

- $\text{sum } \Sigma(u,v) = \int \left| \mathbf{x}_{A_i}(t) + \mathbf{x}_{B_j}(t) \right|^2 dt$

- $m(u,v) = \frac{\int \left| \mathbf{x}_{A_i}(t) - \mathbf{x}_{B_j}(t) \right|^2 dt}{\int \left| \mathbf{x}_{A_i}(t) + \mathbf{x}_{B_j}(t) \right|^2 dt}$

Sensor  
Geometry (u)



Measurement Plane (v)

## Is a subsurface target present?

Inspect the **sum** value matrix. The presence of the subsurface target is reflected as high sum values for some measurement planes.

## Is the subsurface target symmetric?

Inspect the **m** value matrix. Low *m* values for all sensor geometries when measurement plane aligns with plane of target symmetry.



# Experiments in Sandbox



- Targets used in sandbox experiments
  - Styrofoam Disc.
  - Rock.
  - Crushed Milk Jug.

Wooden Mounting Board

Antenna

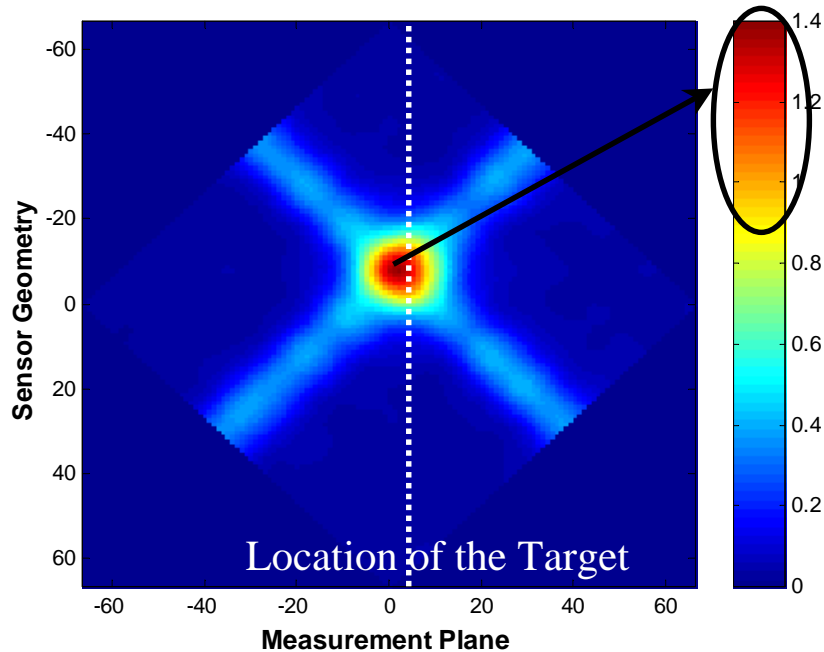


- Data Processing
  - Matched Filter – radar response as function of time
  - Form  $m$  values and sum values matrices
  - Generate color-coded plots.

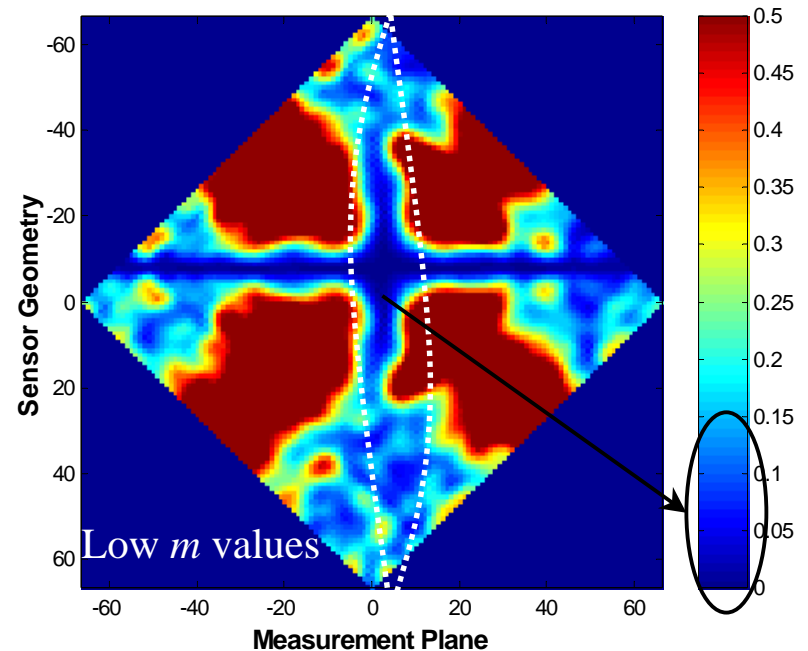




# Styrofoam Disc



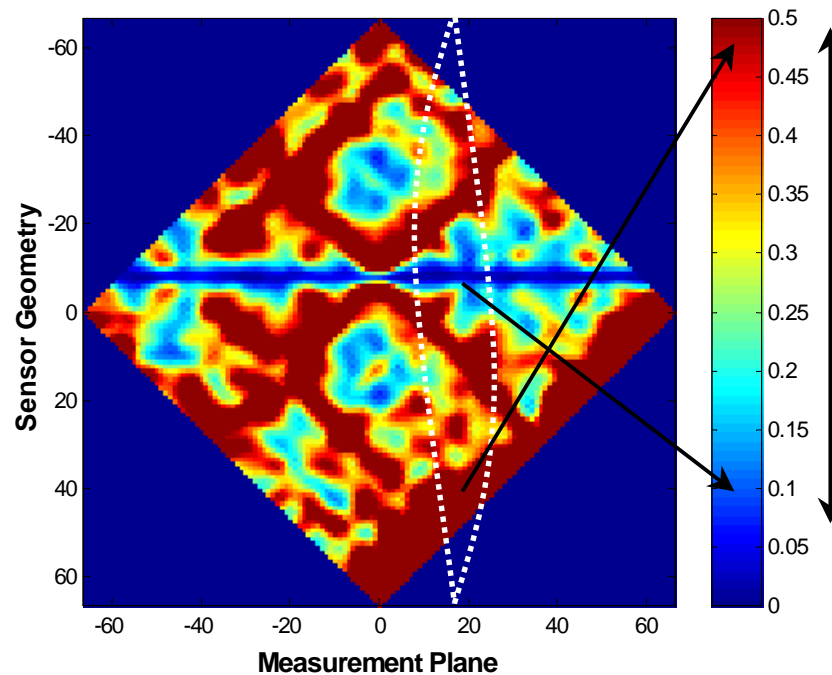
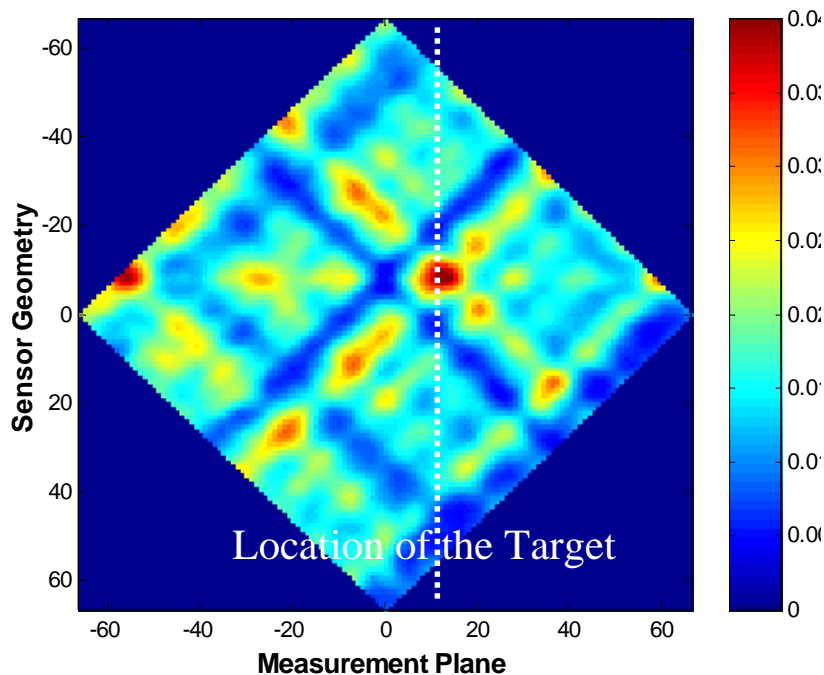
Sum plot indicates presence of the subsurface target!



$m$  plot indicates the subsurface target is symmetric.



# Crushed Milk Jug



Sum plot indicates presence of the subsurface target!

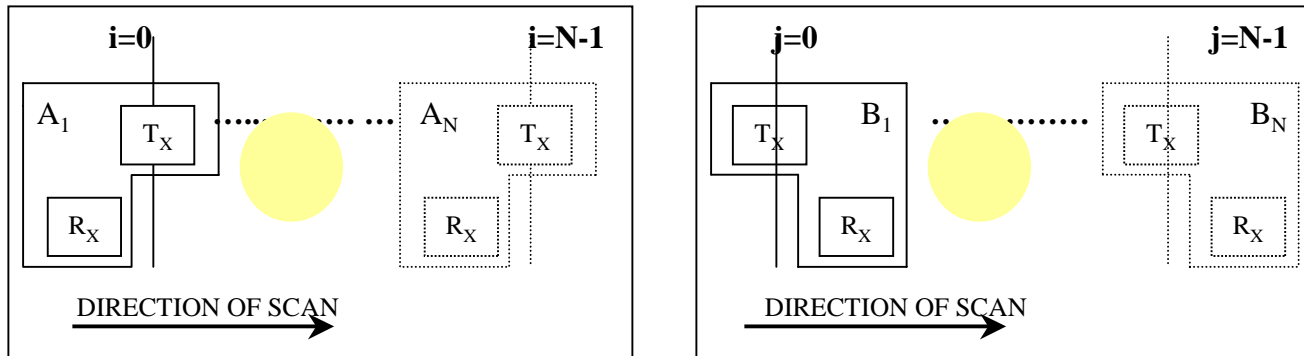
$m$  plot indicates the subsurface target is clutter.



# Sensor Array



- A sensor array can be synthesized using the data collected



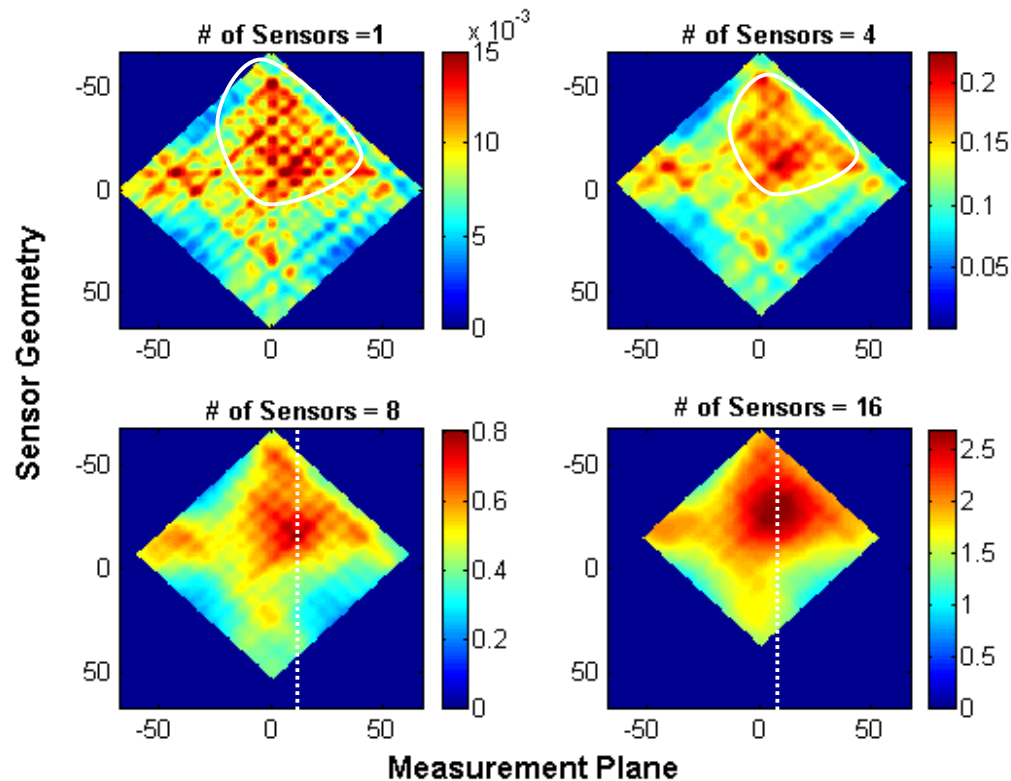
$$x^c_{A_i} = \sum_{k=i}^{i+K-1} x^c_{A_k}$$
$$x^c_{B_j} = \sum_{k=j}^{j+K-1} x^c_{B_k}$$



# Sensor Array Processing



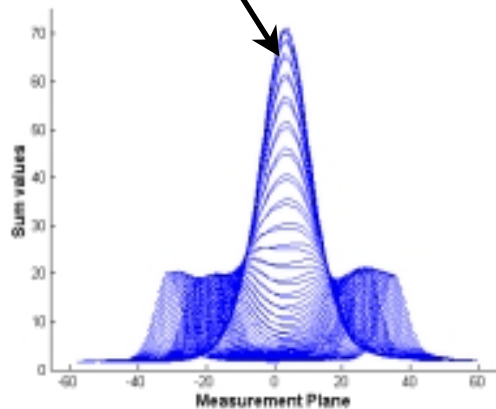
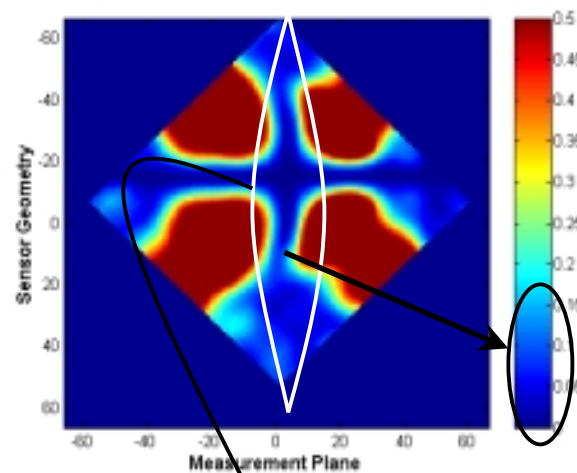
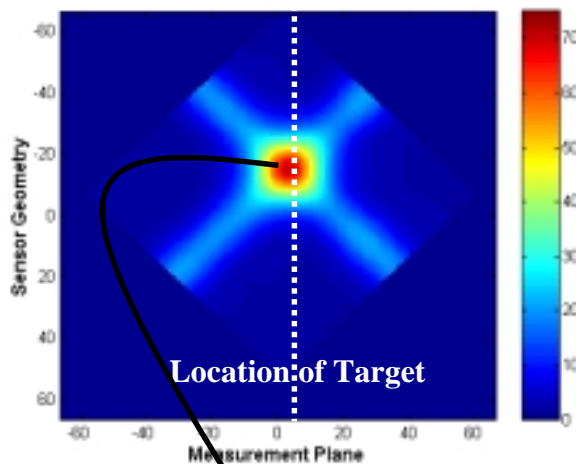
## VAL-69 Antipersonnel Mine



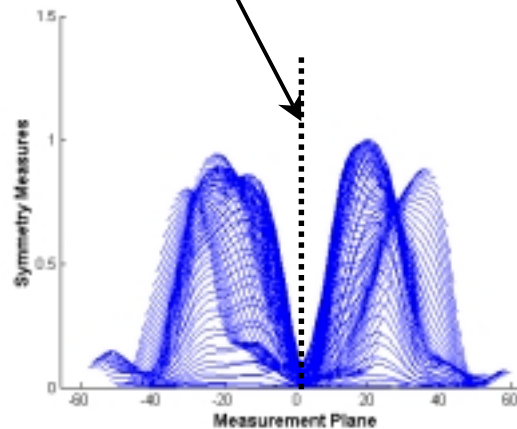
Sensor array with 8 or 16 sensors solves the uncertainty in target detection.



# Sandbox Experiment Styrofoam Disc



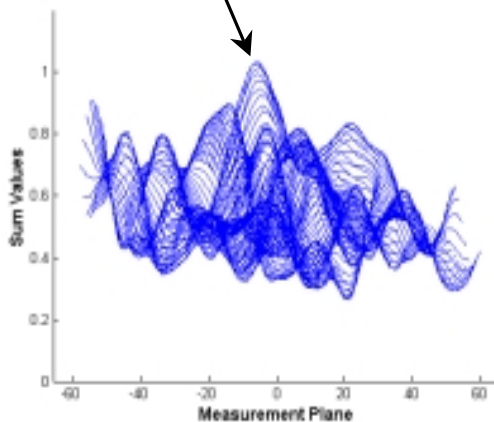
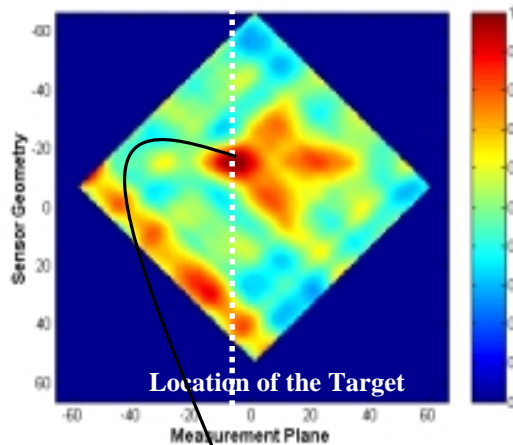
Sum plot indicates  
presence of target



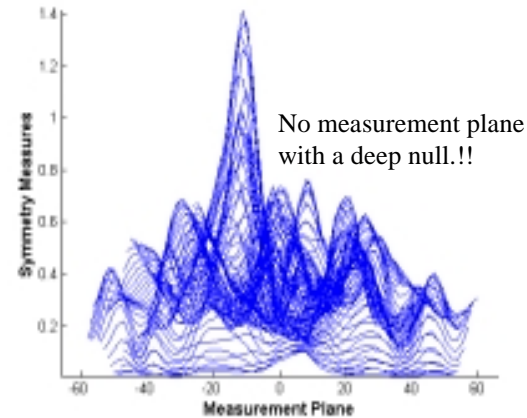
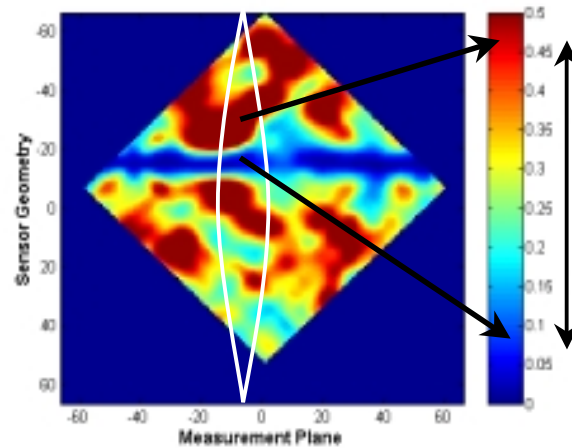
*m* plot indicates that  
target is a symmetric



# Sandbox Experiment-Rock



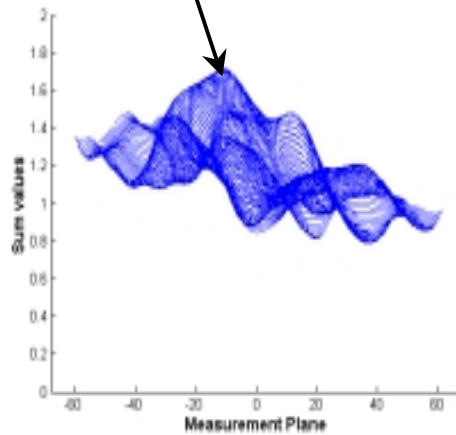
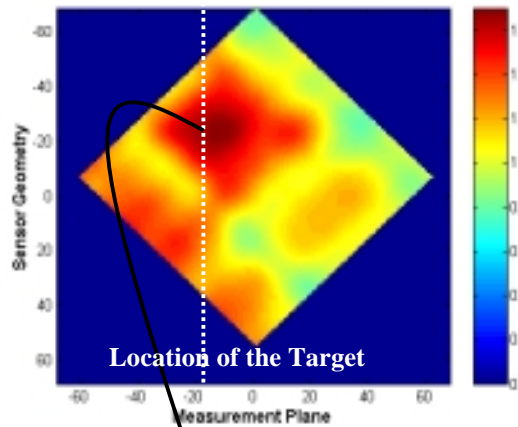
Sum plot indicates presence of target



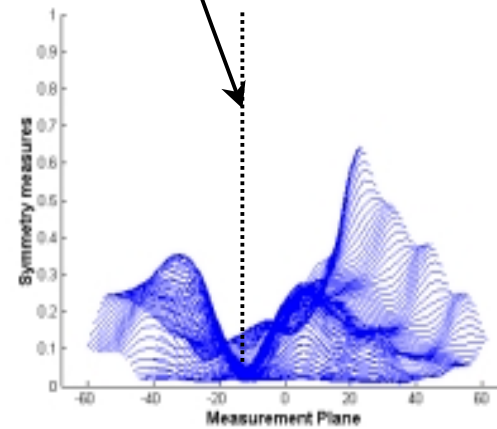
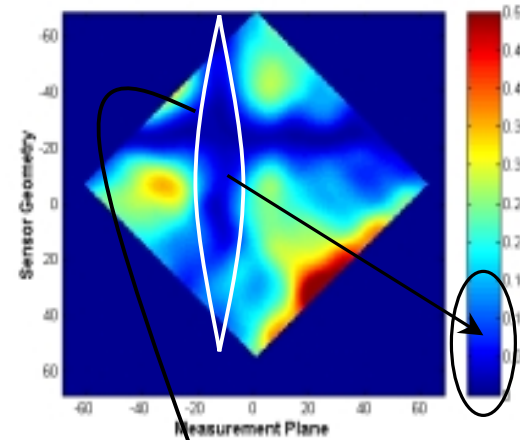
$m$  plot indicates that target is a clutter



# Field Experiment PMA-3



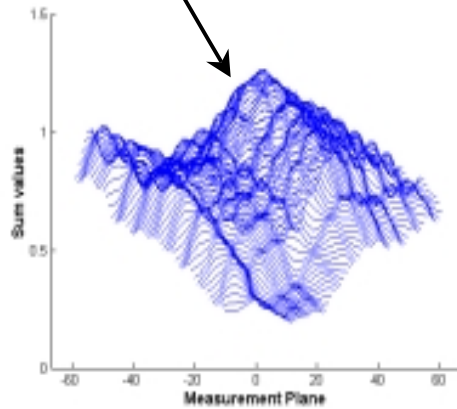
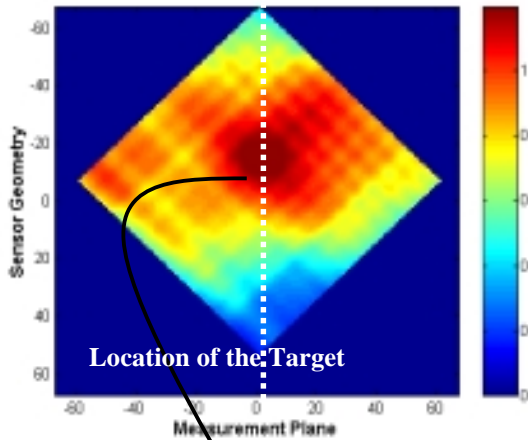
Sum plot indicates presence of target



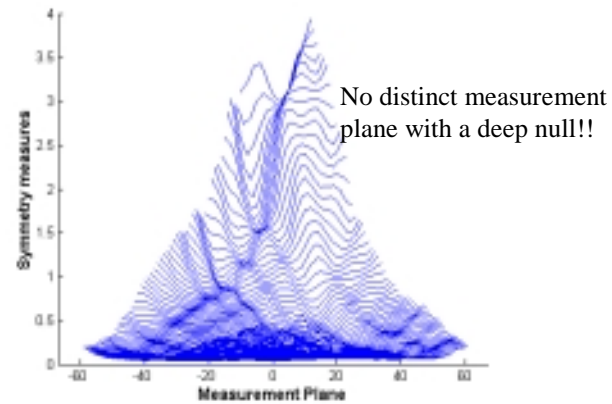
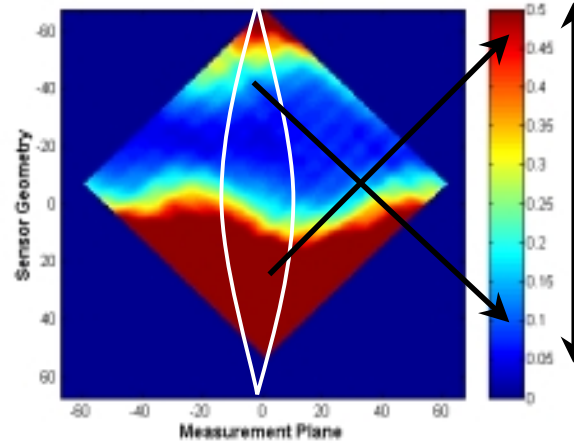
$m$  plot indicates that target is a mine



# Field Experiment Irregular Wood



Sum plot indicates  
presence of target

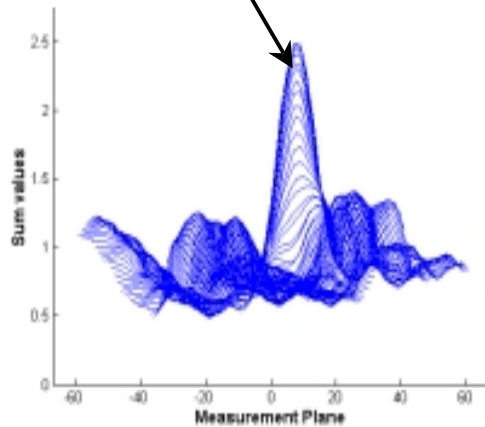
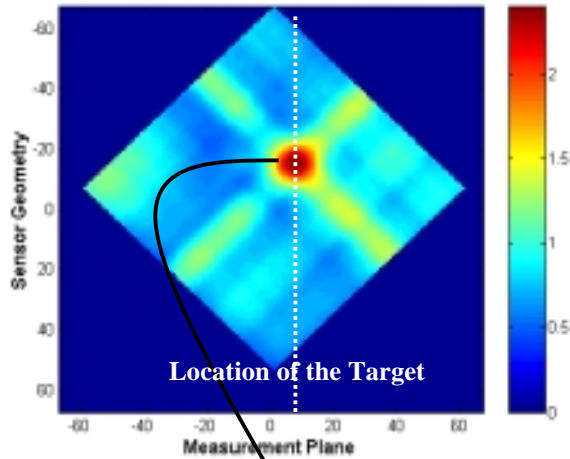


$m$  plot indicates  
that target is clutter

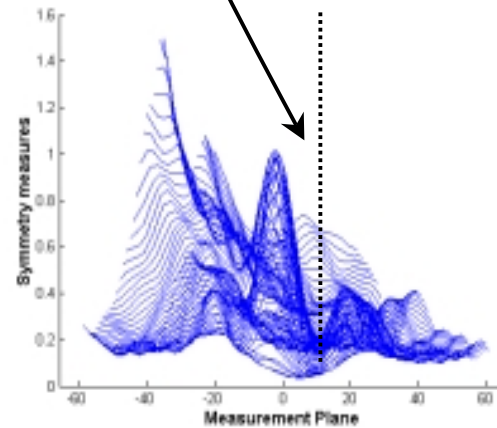
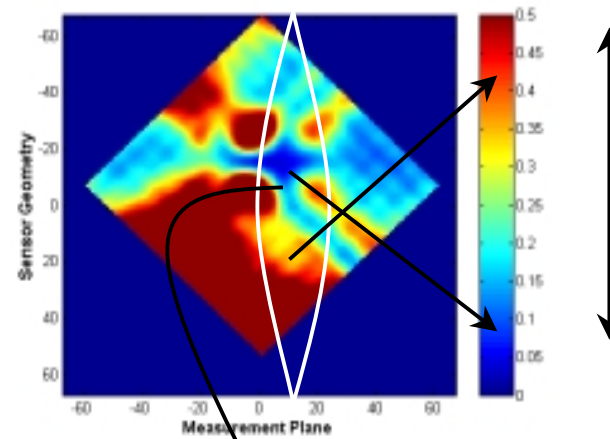




# Field Experiment TM-46



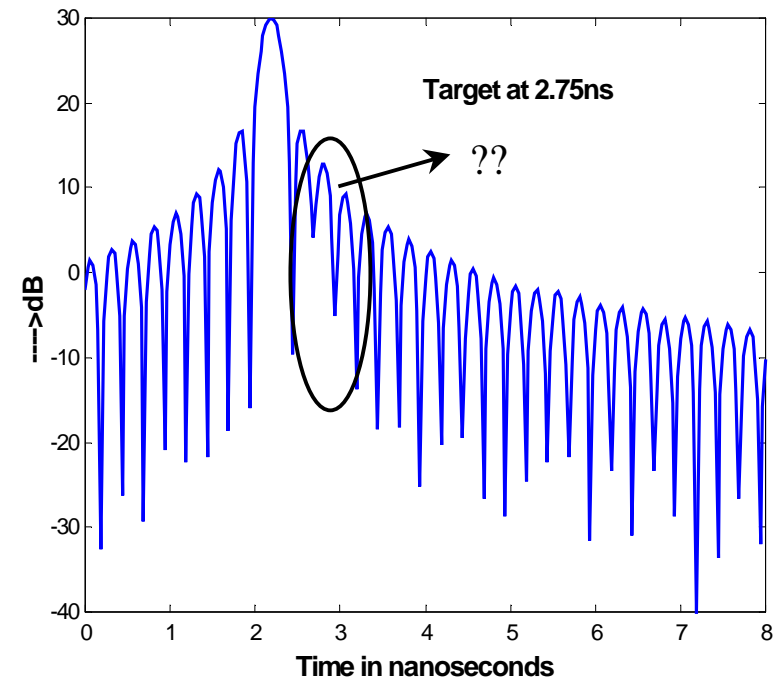
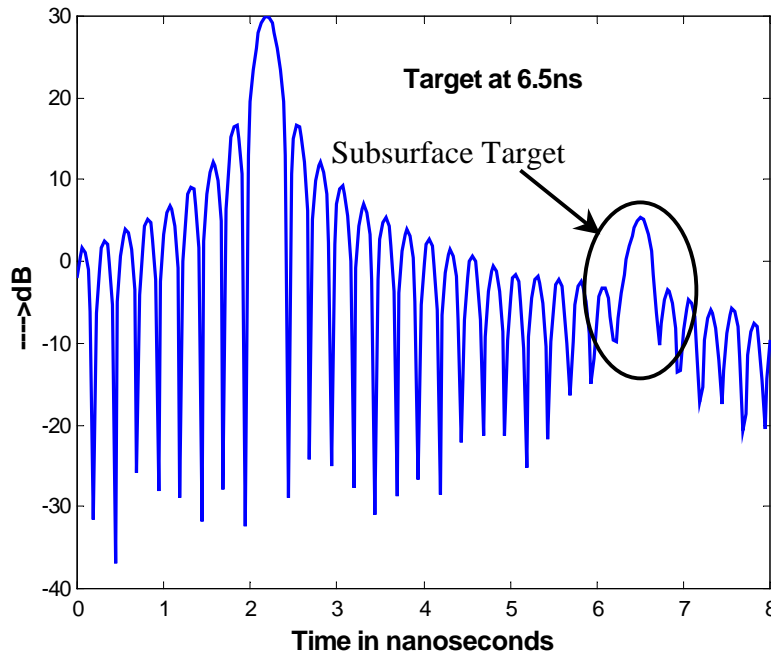
Sum plot indicates presence of target



Is the subsurface target a mine or clutter?



# Matched Filter



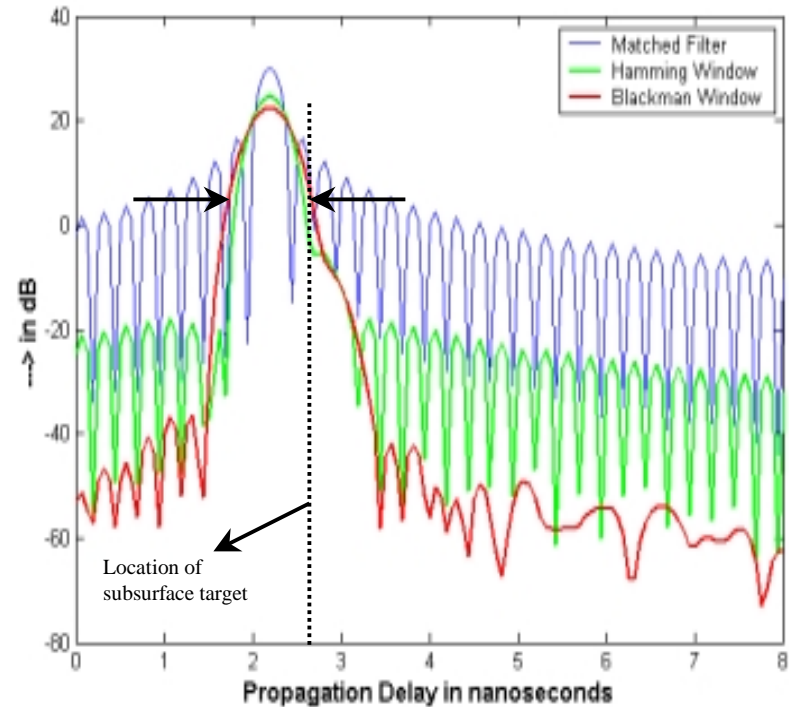
- Time domain side lobes mask subsurface target.
- Can a better signal processing algorithm be developed?



# Optimum Signal Processing Algorithms



- Conventional solution
  - Use Windowing Functions.
  - Is it an efficient solution?
- Motivation
  - Interference dominated by clutter....not by noise.
  - Matched Filter maximizes SNR.
  - Criterion: Maximize SIR



Basis for developing a robust signal processor:  
*a priori* information about the scattering scenario.



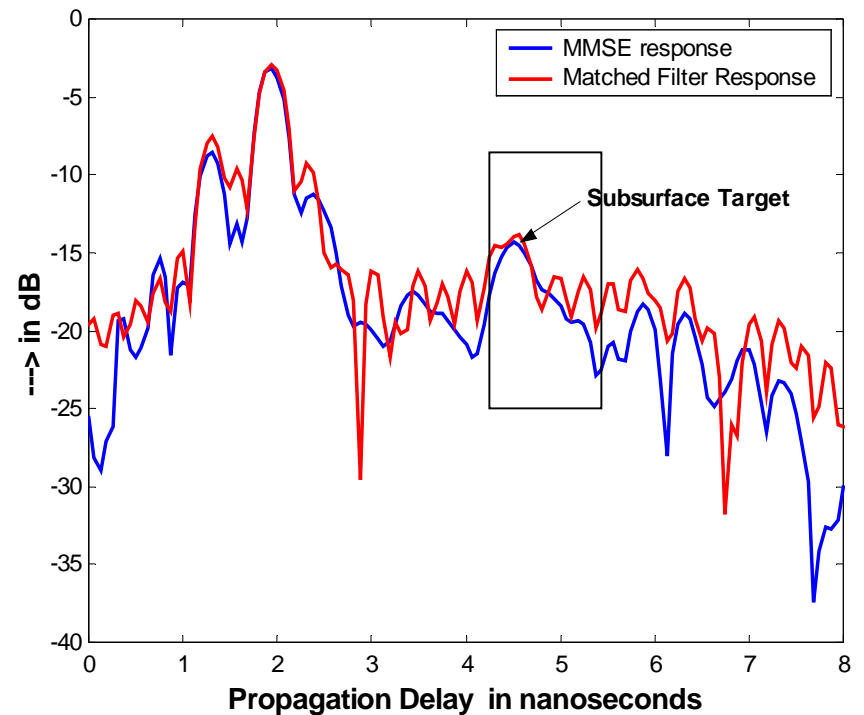
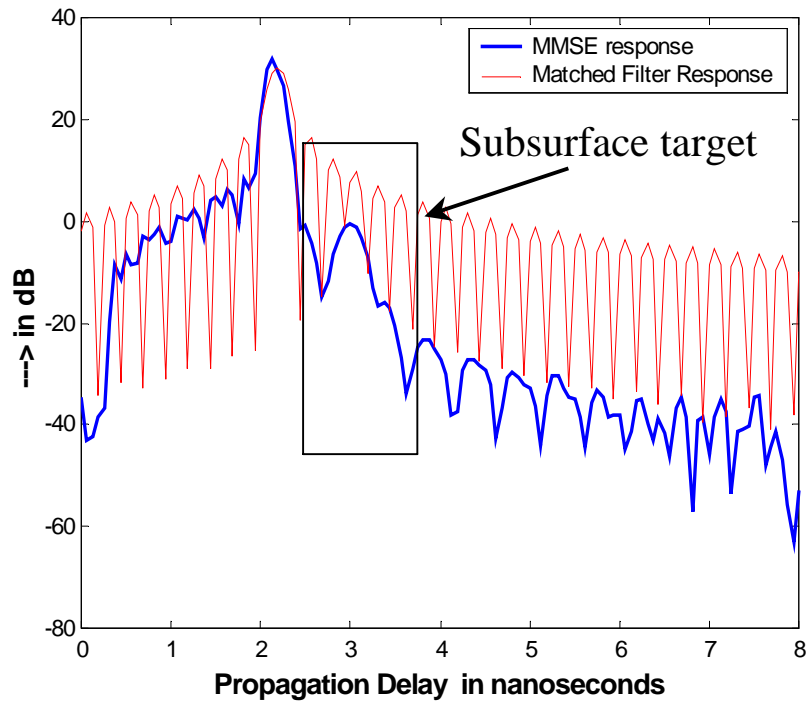
# MMSE GPR Processor



- Radar Response Model:  $\mathbf{r} = \sum_j \gamma_j \boldsymbol{\rho}_j + \mathbf{n}$ 
  - Using Linear Algebra  $\mathbf{r} = \mathbf{P} \boldsymbol{\gamma} + \mathbf{n}$  where  $\mathbf{P}$  is the expected response matrix.
- The estimate of scattering  $\hat{\boldsymbol{\gamma}} = \mathbf{W}_{\text{EST}} \mathbf{r}$
- The criterion to be minimized  $\boldsymbol{\varepsilon} = \hat{\boldsymbol{\gamma}} - \boldsymbol{\gamma}$
- The MMSE Estimator  $\mathbf{W}_{\text{EST}} = \mathbf{K}_{\boldsymbol{\gamma}} \mathbf{P}' [\mathbf{P} \mathbf{K}_{\boldsymbol{\gamma}} \mathbf{P}' + \mathbf{K}_n]^{-1}$ 
  - $\mathbf{W}_{\text{EST}}$  is the MMSE Estimator.
  - $\mathbf{K}_{\boldsymbol{\gamma}} = \mathbf{E} \{ \boldsymbol{\gamma} \boldsymbol{\gamma}' \}$  is the target correlation matrix.
  - $\mathbf{K}_n$  is the noise covariance matrix.



# Results



MMSE GPR processor performs better than Matched Filter.

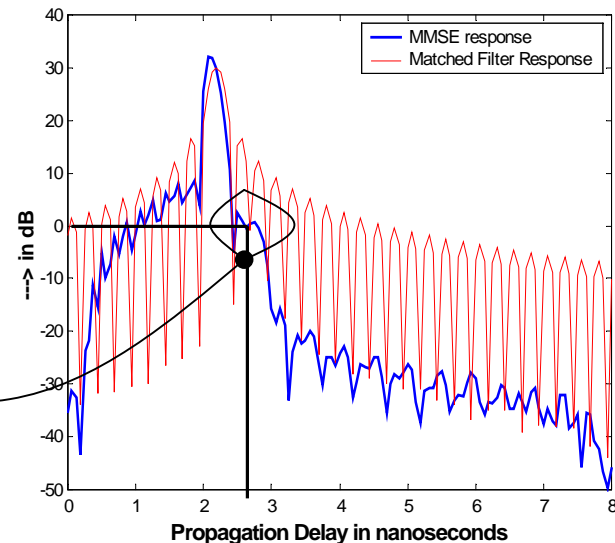


# MMSE GPR Processor-Summary



- MMSE GPR Processor
  - Reduces the effects of surface clutter on subsurface scattering.
  - Maximizes SIR, performs better than Matched Filter.
  - Gives accurate estimates of scattering.
- Problems with the MMSE GPR Processor
  - Time consuming algorithm.
  - If target buried at very shallow depths.

Subsurface Target ??





# Kalman Filter Implementation



- Motivation
  - Reduce processing time.
  - Performance improvement.
- Kalman Filter based on two fundamental equations
  - State Equation :  $x(m + 1) = A(m)x(m) + u(m)$
  - Observation Equation:  $y(m) = C(m)x(m) + n_1(m)$
- Develop a Kalman filter for our application.



# Kalman Filter Algorithm



$$K_{\gamma}(m | m - 1) = K_{\gamma}(m - 1 | m - 1) + K_u(m)$$

$$K_{\gamma}(m) = E\{\gamma(m)\gamma'(m)\} \quad K_u(m) = E\{u(m)u'(m)\}$$

Error Covariance Matrix

The Kalman Gain

$$G(m) = K_{\gamma}(m)P'(m)[P(m)K_{\gamma}(m | m - 1)P'(m) + K_n(m)]^{-1}$$

The innovation Process

$$v(m) = r(m) - P(m)\hat{\gamma}(m - 1 | m - 1)$$

The Estimate of Scattering

$$\hat{\gamma}(m | m) = \hat{\gamma}(m - 1 | m - 1) + G(m)v(m)$$

$$K_{\gamma}(m | m) = [I - G(m)P(m)]K_{\gamma}(m | m - 1)$$

Initial Condition have to be set to initiate the Kalman Filter





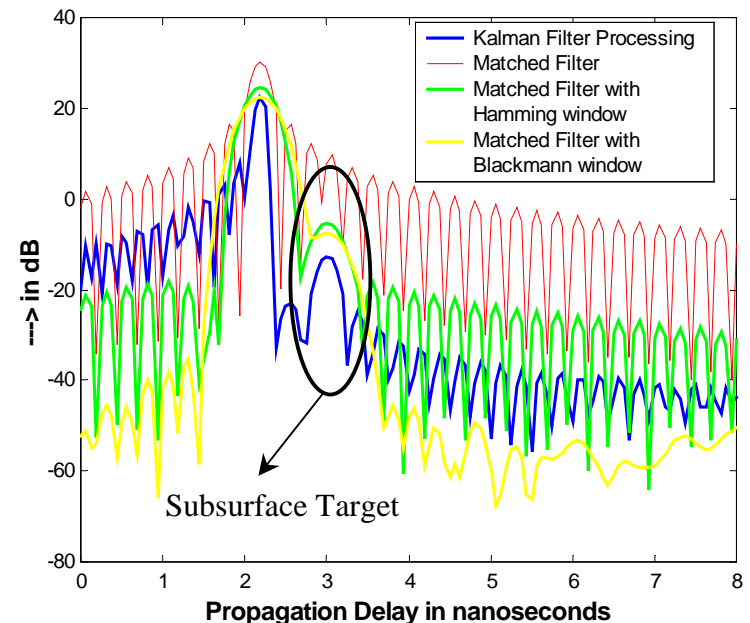
# Simulations



- Initial Conditions set for
  - Error Covariance Matrix
  - Target Correlation matrix
  - Initial Scattering
- Optimum length of radar data segment: One

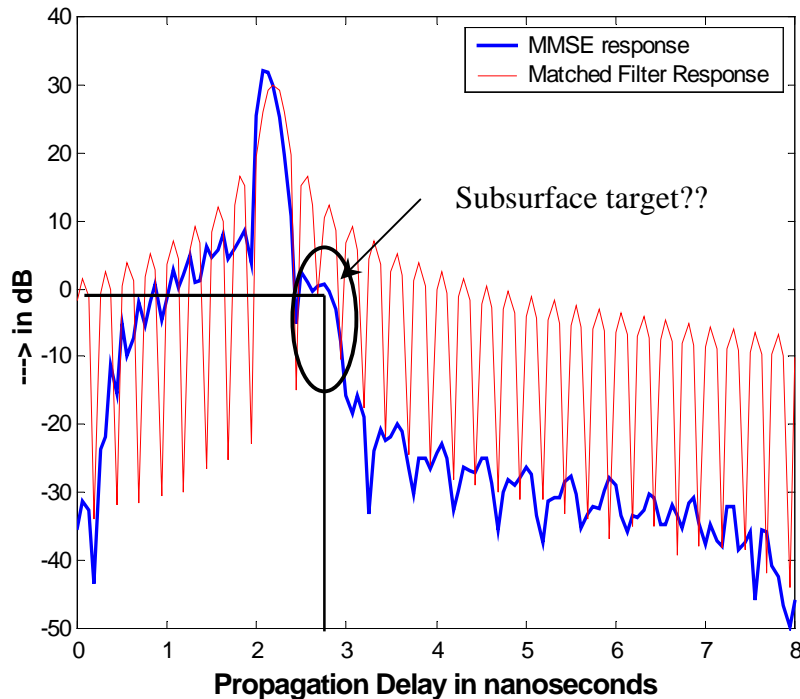
Kalman Filter performs better than Matched Filter.

How is this a performance improvement over MMSE GPR Processor?

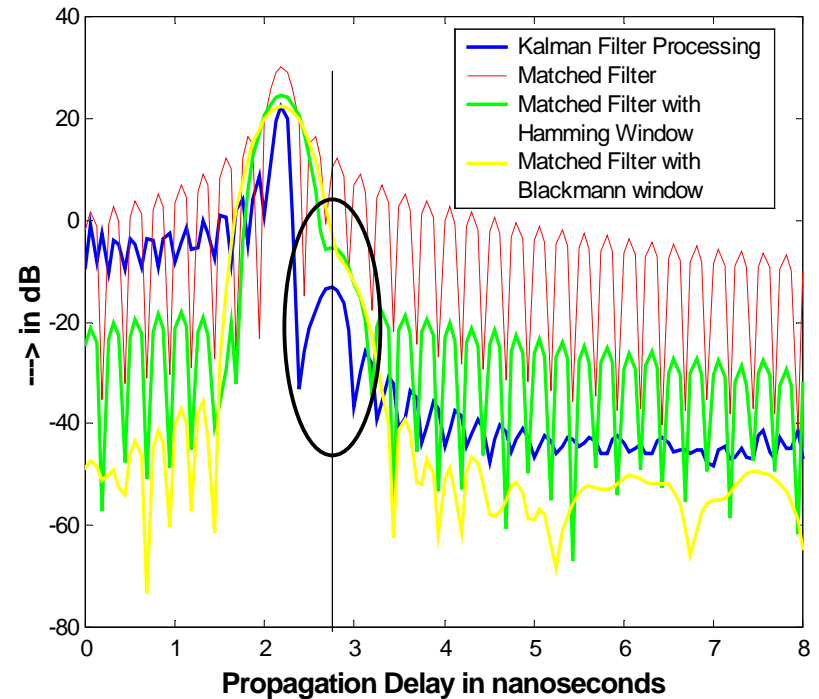




# Simulation Results



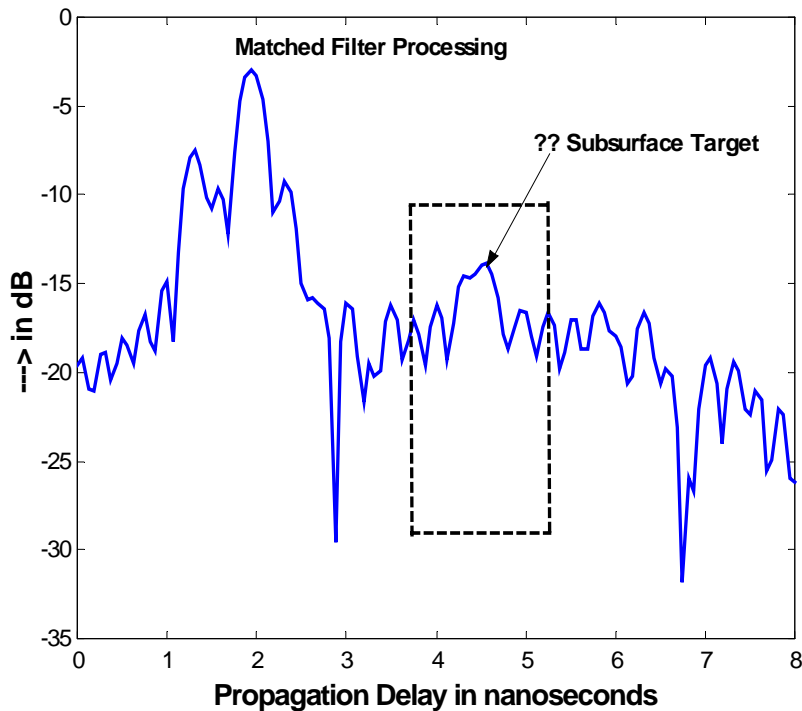
MMSE Filter: Subsurface target at 2.75ns??



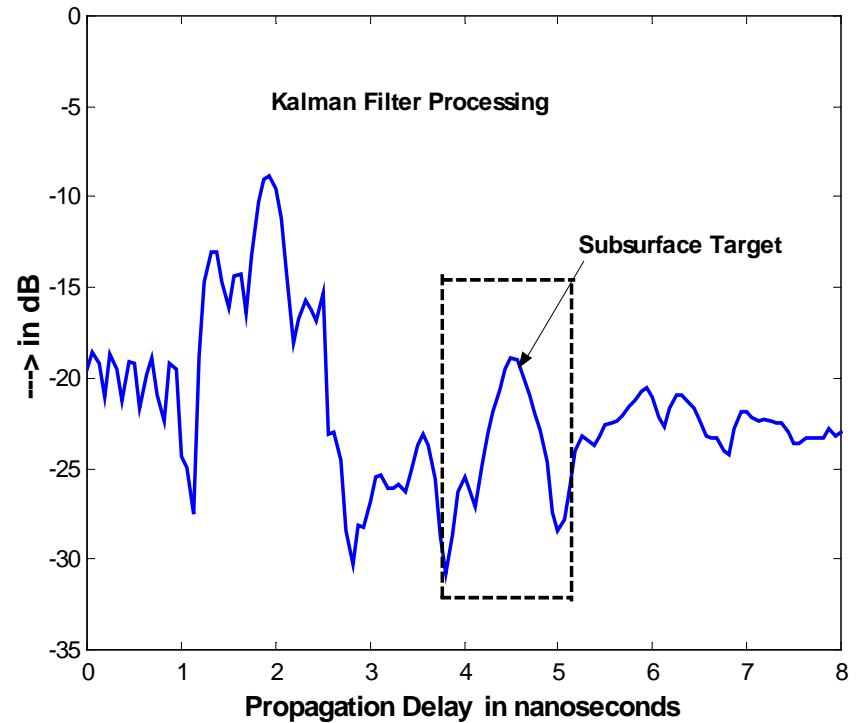
Kalman Filter: Robust for target detection.



# TM-46



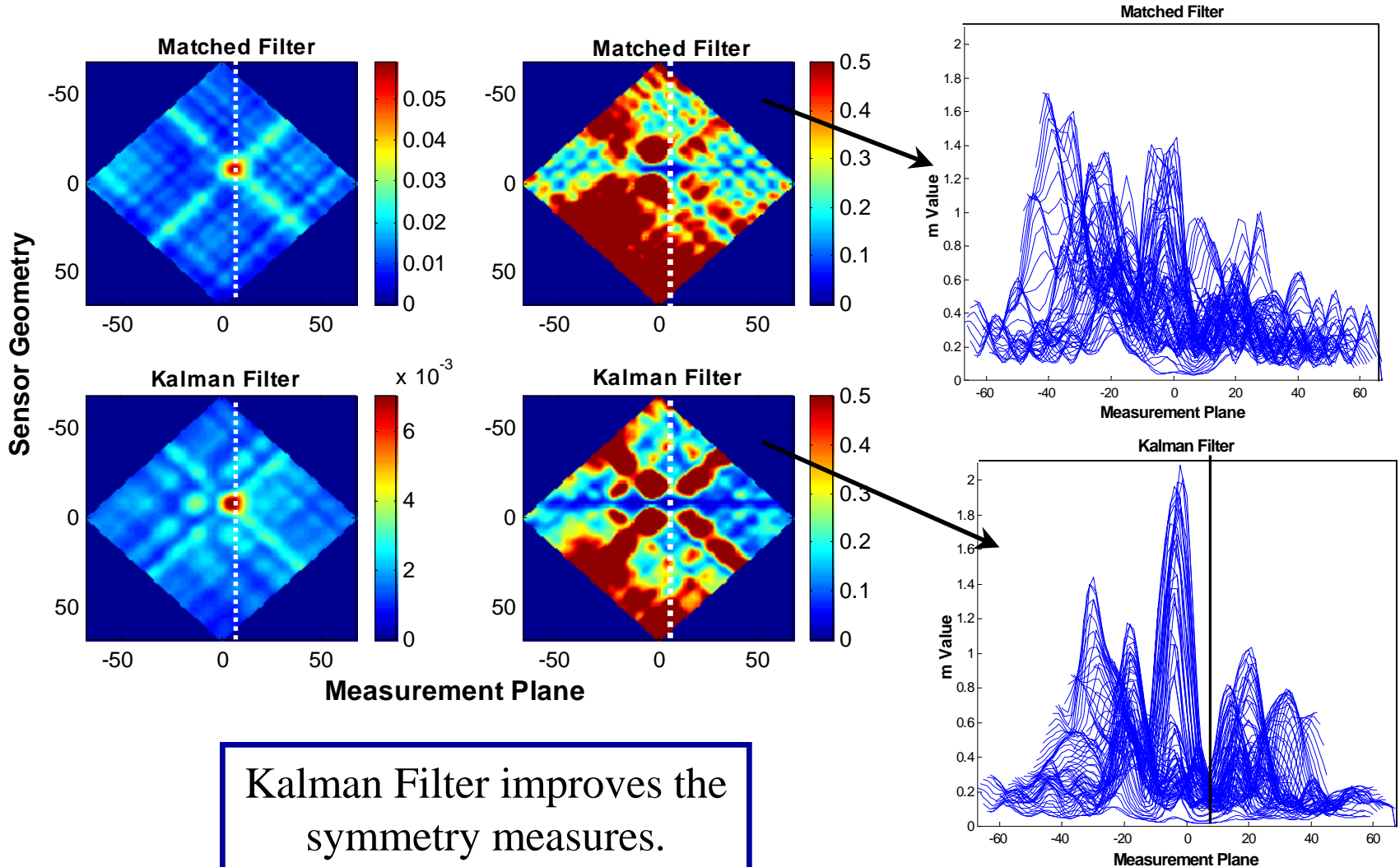
Matched Filter: Uncertainty  
in Target detection



Target can be easily  
detected at a delay  $\approx 4.5$  ns



# TM-46





## Conclusions and Future Work



- Detection Scheme with a potential of a low  $P_{FA}$ .
- Proposed a working model for a handheld detector.
- On the signal processing front
  - Developed a robust signal processor for subsurface target detection.
  - Validated and tested the algorithms.
- As future work
  - Combination of MMSE GPR Processor and Kalman Filter.
  - Develop a Robotic arm for data collection!



Questions?



